EXAM 1: Statistics 100

## Cover Sheet Questions (1 pt.)

1) What's your name? $\qquad$
(Last name)
(First name)
2) What's your net ID (email)? $\qquad$
3) Which Section are you in?
Circle one:
i) L 1 (MWF at 12 pm )
ii) L2 (Tues/Thurs 11am)
iii) ONLINE

Write answers in appropriate blanks. All multiple-choice questions have exactly one answer. If you circle more than one answer you will automatically be marked wrong.
*SHOW WORK when requested, otherwise no credit. Do NOT use scrap paper.
Make sure you have all 6 pages including the normal table ( 10 problems).

## DO NOT WRITE BELOW THIS LINE

The numbers written in each blank below indicate how many points you missed on each page. The numbers printed to the right of each blank indicate how many points each page is worth.

Page 1 $\qquad$ 16

Page 2 $\qquad$ 16

Page 3 $\qquad$ 15

Page 4 $\qquad$ 23

Page 5 $\qquad$ 29

Cover Page $\qquad$ 1

WARNING- The exams look alike but you are sitting next to people who actually have a different version than you. Copying from anyone is equivalent to giving a signed confession.

All cheating including being caught with a nonpermissible calculator or formula sheet will result in a 0 and an academic integrity violation on your University record.

1 pt. for answering cover page questions
1-3 correctly!
Total Score $\qquad$

There is NO CLASS on Thursday or Friday!
Scores will be posted on Compass by Friday morning and exams will be returned in class next week. Online students may pick up their exam in 23
Illini Hall during office hours next week.

Question 1 (9 points total) A recent study was done to examine the possible health benefits of broccoli. The study looked at children who ate broccoli at least once per week and compared them to children who rarely, if ever, ate broccoli. The study followed the children into adulthood and found that the broccoli group had a significantly lower rate of obesity than the nonbroccoli eating group.
a) (1 pt.) What type of study is this? Choose one: i) Randomized Controlled Experiment ii) Observational Study
b) (2 pts.) My husband hates eating broccoli! Based only on the given information, can you conclude that I should tell him that broccoli (his worst enemy!) caused the children to have a lower rate of obesity? Choose one:
i) Yes, this study provides strong evidence that eating broccoli as a child does help prevent obesity in adulthood.
ii) Yes, because the study compared a treatment group (broccoli eaters) to a control group (non-broccoli eaters), it's appropriate to conclude that there is a causal relationship.
iii) No, we can only conclude that eating broccoli is associated with lower obesity rates. It may or may not be the cause.
iv) No, because the parents were in charge of giving the children broccoli, there is no way that this relationship can possibly be causal.
c) Below are either possible causal links, confounders or neither. (Choose answer based only on given info.)
i) (2 pts.) Genetics: Due to their family history, certain individuals are more genetically prone to obesity than others regardless of if they eat broccoli or not.
Choose one:
a) Causal Link
b) Confounder
c) Neither
ii) (2 pts.) Vitamins: Broccoli contains high levels of vitamin A and vitamin C. Both of which help maintain a healthy and functional metabolism. The better your metabolism, the less likely you are to become obese.
Choose one:
a) Causal Link
b) Confounder
c) Neither
iii) (2 pts.) Healthy Habits: Children whose parents encourage healthy habits are more likely to be encouraged to eat broccoli, as well as exercise regularly and eat healthy in general, both of which decrease the probability of becoming obese in adulthood.
Choose one:
a) Causal Link
b) Confounder
c) Neither

Question 2 (7 points total) Suppose McKinley Health Center wanted to do an experiment to see if taking vitamins prevent students at U of I from getting colds. They decide to randomly divide 200 volunteers into two groups: Group 1 takes a multivitamin every day for the entire academic year and Group 2 takes a water pill that looks like a vitamin. Neither the volunteers nor the doctors at McKinley know who's in each group.
a) (1 pt.) How would you best describe this study? Choose one:
i) Randomized Double-Blind Experiment ii) Non-Randomized Experiment with a placebo iii) Observational Study
b) (2 pts.) What kind of bias will be present in this experimental design? Choose one:
i) Subject Bias- the volunteers knew which group they were.
ii) Evaluator Bias- the evaluators could tell which group the volunteers were in
iii) Both Subject and Evaluator Bias
iv) Selection Bias- the volunteers decided which group they were in
v) None of the above types of bias
c) (2 pts.) Will there be confounders that the researchers will have to adjust for? Choose one:
i) Yes, anytime you do any study confounders will be present.
ii) No, group 1 and group 2 will be as alike as possible.
iii) Maybe, it depends on the results of the study.
d) (2 pts.) What comparison do we make at the end if people stop taking their vitamins? Choose one:
i) Compare everyone in treatment to everyone in control to keep the original randomization
ii) Only compare those who took their vitamins (adherers) to those who took the water pill (adherers).
iii) Compare those who took their vitamins (adherers) to those who didn't take their vitamins (non-adherers).

Question 3 (2 pts.) There are two sections of Stat 100 this semester. One meets 3 times per week (MWF class) and the other meets 2 times per week (Tues/Thurs class). Which is better for learning? In order to come to a conclusion, I'd have to design an experiment. Which of the following would be best? Choose one
a) Allow all Stat 100 students to decide which section they think will be best for them and register for that section. At the end of the semester, compare the grades of the MWF class and Tues/Thurs class to see who did better.
b) Put all of next semester's Stat 100 students in a MWF class and compare their grades to this semester's Tues/Thurs section to see who has a higher average.
c) Randomly assign half of the Stat 100 students to the MWF class and the other half to the Tues/Thurs class. At the end of the semester, compare the averages of both classes.
d) Give all of the students a math test. Take the students who score highest and put them in the Tues/Thurs class and then take the rest of the students and put them in the MWF class since they'll probably need to see the material 3 times per week. At the end of the semester, compare the grades of the two sections.

Question 4 (5 points total) ABC 7 Chicago recently reported on a study that said that people who drink a glass of wine each night are less likely to be overweight than those who don't. The title of the article was "Drinking a glass of wine each night is equivalent to going to the gym for an hour."
a) (l pt.) This is an example of $\mathrm{a} . .$. Choose one: i) Observational study ii) Randomized Controlled Experiment
b) (2 pts.) Say I thought household income could be a confounder because people with high incomes are both more likely to drink a glass of wine each night and have a gym membership to help keep their weight down. How could I check to see if household income is a confounder?
i) At the beginning of the study, divide the subjects into subgroups based on whether or not they drink wine and then at the end of the study compare their weights.
ii) At the beginning of the study, divide the subjects into subgroups based on income and then at the end of the study, compare the amount of wine each income group drank
iii) At the end of the study, divide the subjects into subgroups based on age and compare their weights of the younger subjects who drank wine to the older subjects who drank wine.
iv) At the end of the study, divide the subjects into subgroups based on income and compare the weights of the highincome subjects who drank wine to the high-income subjects who did not. Do the same for the low-income subjects.
c) (2 pts.) Based only on the given information, which of the following could confound the results?
i) Alcohol- wine contains alcohol, which is known to help build muscle mass. This is why people who drink wine are in better shape than those who don't.
ii) Good Health- people who are in good health are more likely to go to the gym and drink a glass of wine with dinner each night.
iii) Grapes- wine contains grapes which are a fruit high in antioxidants. Eating fruit helps people get in better shape.
iv) There should not be any confounders in this type of experiment.

Question 5 ( 9 pts. total) pertains to the following list of 6 numbers: $1,-4,-3,4,3,5$
a) (2 pts.) The average is $\qquad$ and the median is $\qquad$
b) (3 pts.) The deviations from the average are $\qquad$ , $\qquad$ , $\qquad$ , $\qquad$
c) (2 pts.) The sum of the deviations from the average should $=$ $\qquad$ . Fill in the blank with a number.
d) (2 pts.) Compute the Standard Deviation and circle your final answer. Round your answer to 2 decimal places. No work, no credit. You may start with the deviations you found in part (b).

Question 6 (5 pts. total) Two different types of treatment are being used against tumors. After an extensive study, here are the results in the table below.

|  | Treatment A |  | Treatment B |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Number | Success Rate | Number | Success Rate |
| Small Tumors | 65 | $92 \%$ | 16 | $94 \%$ |
| Large Tumors | 35 | $71 \%$ | 84 | $76 \%$ |
| Total | 100 | $85 \%$ | 100 | $79 \%$ |

a) (1 pt.) Which treatment is better for small tumors?
Choose one:
i) Treatment A
ii) Treatment B
iii) Unknown
b) (1 pt.) Which treatment is better for large tumors?
Choose one:
i) Treatment $A$
ii) Treatment B
iii) Unknown
c) (1 pt.) Which is treatment is better overall?

Choose one: $\begin{array}{llll}\text { i) Treatment A } & \text { ii) Treatment B } & \text { iii) Unknown }\end{array}$
d) (2 pts.) What is the best conclusion based on the data above? Choose one:
i) It's impossible to make a decision because there is probably a mathematical error when calculating the percentages.
ii) It's clear that treatment A is better because we always want to compare the overall percentages when making a conclusion from a study.
iii) Treatment B is better because if we look individually at both large tumors and small tumors, it has the higher success rate.
iv) Treatments A and B both work equally well because one works better individually, and one works better overall.

Question 7 (10 pts. total) A recent survey asked college students majoring in statistics how many hours per week they spend on homework. The results are summarized in the table below.
a) ( 5 pts .) Fill in the $\mathbf{4}$ blanks in the table below:

| Hours | Area \% | Height of Block <br> (\% per hour) |
| :--- | :--- | :--- |
| $0-2$ | 8 | $(1 \mathrm{pt})$ |
| $2-4$ | 12 | 6 |
| $4-6$ | 20 | $(1 \mathrm{pt})$. |
| $6-8$ | 24 | $(1 \mathrm{pt})$. |
| $8-12$ | $(1 \mathrm{pt})$. |  |

b) (2 pts.) Draw the histogram on the graph below.
\% per
hour

c) (2 pts.) What value represents the $40^{\text {th }}$ percentile? $\qquad$
d) (1 pt.) The number of people who answered 0-6 hours is $\qquad$ the number of people who answered 6-12 hours.
Choose one:
i) less than
ii) more than
iii) the same as

Question 8 (10 points total) Answer the following questions about measures of center and spread:
a) (3 pts.) Consider this list of numbers: $\mathbf{1}, \mathbf{1}, \mathbf{1}, \mathbf{1}, \mathbf{1}$. Fill in the 3 blanks below with numbers.
v) What is the average? $\qquad$ ii) What is the median? $\qquad$ iii) What is the SD? $\qquad$
b) (3 pts.) If the SD of a list of numbers is 1, which of the following is true? Circle True or False for each part.
i) The average must be 1

True False
ii) All the numbers must be the same

True
False
iii) If I add 1 to every number, the SD of the list is 2

True
False
c) Minions have an average weight of 1000 g and a standard deviation of 50 g . Use this information for both parts $1 \& 2$.

Part 1: If every minion eats a 100 g banana, what is the new average weight and standard deviation of minions (immediately after eating)? Fill in the blanks with NUMBERS, not words.
(1 pt.) Average $\qquad$ g
(1 pt.) SD $\qquad$ g

Part 2: Instead of eating a banana, the minions go to Mars, where the gravity is only $40 \%$ of Earth's (in other words, weight on Mars $=0.4^{*}$ Weight on Earth). Ex. a 100-pound person on Earth will weigh 40 pounds on Mars.

Assuming the minions have the original average weight $(1000 \mathrm{~g})$ and standard deviation $(50 \mathrm{~g})$ on Earth, what will their average weight and standard deviation be on Mars?
(1 pt.) Average $\qquad$ g
(1 pt.) SD
Question 9 (13 points total) Below is a histogram displaying our survey results to the question: "How many alcoholic beverages do you consume per week on the average?" The 15-30 block is missing. (Assume an even distribution throughout the interval.)
\% Per Drink

a) (4 pts.) Fill in the percentage for each block in the blanks provided on the histogram above.
b) ( 1 pt.) Draw in the missing block accurately in the histogram above.
i) (1 pt.) What is the area of the block? $\qquad$ \%
ii) (1 pt.) What is the height of the block_ $\%$ per drink.
c) (2 pts.) What percentage of students reported consuming exactly 12 alcoholic beverages per week?
Choose one:
i) $1 \%$
ii) $4 \%$
iii) $8 \%$
iv) $20 \%$
d) (2 pts.) The average is $\qquad$ than the median. Choose one:
i) greater
ii) less
iii) equal
e) (2 pts.) Is it appropriate to use the normal curve as an approximate histogram for this data? Choose one: i) yes b) no

Question 10 (29 points total) The number of hours of sleep that students got on Reading Day is approximately normally distributed with an average of 6.5 hrs . \& an SD of 1.5 hrs . Use the normal approximation to answer the following questions. Show work where it says to or no credit! You may round percentages on the normal table to the nearest whole number.
a) (2 pts.) About $95 \%$ of students got between $\qquad$ \& $\qquad$ hours of sleep on Reading Day.
Show work:
b) (2 pts.) If a student is 1 SD above average, what is their z -score and how many hours of sleep did they get on Reading Day?
z-score= $\qquad$ Hours of Sleep= $\qquad$ Show work:
(no work necessary)
c) (2 pts.) If a student is 0.6 SDs below average, what is their z-score and how many hours of sleep did they get on Reading Day last semester? No work, no credit.
z-score= $\qquad$ Hours of Sleep= $\qquad$ Show work:
(no work necessary)
d) Approximately what percent of students got between 4.7 and 5.6 hours of sleep? No work, no credit.
i) (2 pts.) Translate this interval into Z scores. $\qquad$ to $\qquad$
ii) (1 pt.) Mark the Z scores correctly onto the curve below and shade the corresponding area
iii) (2 pts.) Calculate the percent $\qquad$ \%

e) (3 pts.) One student claimed to sleep for 9.2 hours. What percentile is she in? No work, no credit.
z- score= $\qquad$ percentile= $\qquad$
Mark the z -score on the curve and shade the percentile!

f) (5 pts.) One student is in the $60^{\text {th }}$ percentile. How many hours did they sleep? No work, no credit.

Middle area corresponding to the $60^{\text {th }}$ percentile $=$ $\qquad$ z-score= $\qquad$ value= $\qquad$ hrs.


Mark the z-score on the curve and shade the percentile!
g) (2 pts.) Another student is in the $40^{\text {th }}$ percentile. How many hours did they sleep?
z-score= $\qquad$ , value= $\qquad$ hrs. Show work:
(no work necessary)
h) ( 8 pts.) In the table below, you are given either the Z score or the percentile for 4 students. Fill in the 4 blanks.


## STANDARD NORMAL TABLE



| $\boldsymbol{z}$ | Area |  | $\boldsymbol{z}$ | Area |  | $\boldsymbol{z}$ | Area |
| :---: | :---: | :--- | :---: | :---: | :--- | :---: | :---: |
| 0.00 | 0.00 |  | 1.50 | 86.64 |  | 3.00 | 99.730 |
| 0.05 | 3.99 |  | 1.55 | 87.89 |  | 3.05 | 99.771 |
| 0.10 | 7.97 |  | 1.60 | 89.04 |  | 3.10 | 99.806 |
| 0.15 | 11.92 |  | 1.65 | 90.11 |  | 3.15 | 99.837 |
| 0.20 | 15.85 |  | 1.70 | 91.09 |  | 3.20 | 99.863 |
|  |  |  |  |  |  |  |  |
| 0.25 | 19.74 |  | 1.75 | 91.99 |  | 3.25 | 99.885 |
| 0.30 | 23.58 |  | 1.80 | 92.81 |  | 3.30 | 99.903 |
| 0.35 | 27.37 | 1.85 | 93.57 |  | 3.35 | 99.919 |  |
| 0.40 | 31.08 | 1.90 | 94.26 |  | 3.40 | 99.933 |  |
| 0.45 | 34.73 | 1.95 | 94.88 |  | 3.45 | 99.944 |  |
|  |  |  |  |  |  |  |  |
| 0.50 | 38.29 |  | 2.00 | 95.45 |  | 3.50 | 99.953 |
| 0.55 | 41.77 | 2.05 | 95.96 |  | 3.55 | 99.961 |  |
| 0.60 | 45.15 | 2.10 | 96.43 |  | 3.60 | 99.968 |  |
| 0.65 | 48.43 | 2.15 | 96.84 |  | 3.65 | 99.974 |  |
| 0.70 | 51.61 | 2.20 | 97.22 |  | 3.70 | 99.978 |  |
|  |  |  |  |  |  |  |  |
| 0.75 | 54.67 | 2.25 | 97.56 |  | 3.75 | 99.982 |  |
| 0.80 | 57.63 | 2.30 | 97.86 |  | 3.80 | 99.986 |  |
| 0.85 | 60.47 | 2.35 | 98.12 |  | 3.85 | 99.988 |  |
| 0.90 | 63.19 | 2.40 | 98.36 |  | 3.90 | 99.990 |  |
| 0.95 | 65.79 | 2.45 | 98.57 |  | 3.95 | 99.992 |  |
|  |  |  |  |  |  |  |  |
| 1.00 | 68.27 | 2.50 | 98.76 |  | 4.00 | 99.9937 |  |
| 1.05 | 70.63 | 2.55 | 98.92 |  | 4.05 | 99.9949 |  |
| 1.10 | 72.87 | 2.60 | 99.07 |  | 4.10 | 99.9959 |  |
| 1.15 | 74.99 | 2.65 | 99.20 |  | 4.15 | 99.9967 |  |
| 1.20 | 76.99 | 2.70 | 99.31 | 4.20 | 99.9973 |  |  |
| 1.25 | 78.87 | 2.75 | 99.40 |  | 4.25 | 99.9979 |  |
| 1.30 | 80.64 | 2.80 | 99.49 |  | 4.30 | 99.9983 |  |
| 1.35 | 82.30 | 2.85 | 99.56 |  | 4.35 | 99.9986 |  |
| 1.40 | 83.85 | 2.90 | 99.63 |  | 4.40 | 99.9989 |  |
| 1.45 | 85.29 |  | 2.95 | 99.68 |  | 4.45 | 99.9991 |
|  |  |  |  |  |  |  |  |

